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Bidirectionally tuning Kapitza conductance through the inclusion of substitutional impurities

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We investigate the influence of substitutional impurities on Kapitza conductance at coherent interfaces via non-equilibrium molecular dynamics simulations. The reference interface is comprised of two mass-mismatched Lennard-Jones solids with atomic masses of 40 and 120 amu. Substitutional impurity atoms with varying characteristics, e.g., mass or bond, are arranged about the interface in Gaussian distributions. When the masses of impurities fall outside the atomic masses of the reference materials, substitutional impurities impede interfacial thermal transport; on the other hand, when the impurity masses fall within this range, impurities enhance transport. Local phonon density of states calculations indicate that this observed enhancement can be attributed to a spatial grading of vibrational properties near the interface. Finally, for the range of parameters investigated, we find that the mass of the impurity atoms plays a dominant role as compared to the impurity bond characteristics. © 2012 American Institute of Physics. [http://dx.doi.org/10.1063/1.4757941]

I. INTRODUCTION

In semiconductor materials, phonon mean-free-paths can exceed several hundred nanometers.1,2 In systems where the distance between interfaces is on the order of or less than this length scale, thermal transport properties are dictated as much by the interfaces between materials as they are by the materials themselves.3,4 The efficiency of thermal transport across a solid-solid interface can be described by the interface Kapitza conductance5 or \( h_K \). At a near-ideal interface, i.e., free of defects and compositionally abrupt, Kapitza conductance is inherently limited by the overlap of the phonon spectra of the two solids comprising the interface.5–11 That is, the better matched the vibrational spectra of the materials, the higher the Kapitza conductance. However, other qualities of the interface can influence Kapitza conductance, including interfacial structure,12–22 interfacial chemistry,23–30 and the relative orientation of the constituent materials.12,31–35

With regard to interface structure, deviations from “ideality” can include one or a combination of several unique features, e.g., compositional mixing,9,22 dislocations,16 confined films,21,22 non-crystallinity,13 or nanometer-scale geometric facets.15,18–20 When compared to ideal interfaces, certain combinations of these features have been found to enhance Kapitza conductance,9,21,22 while others have been shown to reduce it.9,13,15,16,18,19 A subset of these studies have demonstrated that careful control over interfacial structure can provide a means of tuning Kapitza conductance.17–22 More specifically, the results of Refs. 17–19 have shown that nanometer-scale geometric facets achieved through quantum-dot patterning17,18 or chemical etching19 can lead to lower realized values of Kapitza conductance as compared to that at nominally flat (compositionally sharp) interfaces. On the other hand, Refs. 20–22 have indicated that careful control over interfacial structure either through nano-patterning20 or the inclusion of a confined thin film21,22 can enhance conductance by way of grading vibrational properties.

In this report, we investigate the influence of substitutional impurities on Kapitza conductance at coherent interfaces via non-equilibrium molecular dynamics (NEMD) simulations. It is shown that the inclusion of impurities in the vicinity of the interface can provide a means of bidirectionally tuning Kapitza conductance. The reference interface is comprised of two mass-mismatched Lennard-Jones solids, with masses \( m_A \) and \( m_B \), and impurities of mass \( m_i \) are arranged symmetrically about the interface in a Gaussian distribution. When \( m_i < m_A \) or \( m_i > m_B \), Kapitza conductance is lower than that at the reference interface, whereas when \( m_A < m_i < m_B \), conductance is higher. This is contrary to the concept of phonon-impurity scattering in the context of thermal conductivity, where the scattering rate (inverse of scattering time) is often described in a form \( \tau_i^{-1} \propto (m_{host} - m_i)/m_{host}^2 \), and impurities always impede thermal transport.26,37 As in previous work investigating the thermal conductivity of alloys,28 we find that the mass of the impurity atoms plays a dominant role as compared to the impurity bond characteristics (strength or radius).

II. COMPUTATIONAL DETAILS

All computational cells were \( 8 \times 8 \times 80 \) face centered cubic conventional unit cells in size and contained 20480 atoms such that size effects were mitigated.28,35 One half of the atoms were A-type and the other half were B-type,

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TABLE I. The maximum impurity concentration (η), distribution full-width half-max (FWHM), number of impurities (ni), impurity atom mass (mi), impurity atom length parameter (σi), impurity atom energy parameter (εi), and mean and standard deviations of Kapitza conductances at 30 K (hK and ΣK, respectively). Standard deviations increased slightly with increasing simulation temperature and were near to zero at low temperatures.

<table>
<thead>
<tr>
<th>Sample</th>
<th>η (%)</th>
<th>FWHM (nm)</th>
<th>ni (amu)</th>
<th>mi (Å)</th>
<th>εi (eV)</th>
<th>hK at 30 K (W m⁻² K⁻¹)</th>
<th>ΣK at 30 K (W m⁻² K⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Baseline</td>
<td>A 0</td>
<td>10 54</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>97.7</td>
<td>6.4</td>
<td></td>
</tr>
<tr>
<td>Distribution series</td>
<td>B 10</td>
<td>10 54</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>76.9</td>
<td>11.0</td>
<td></td>
</tr>
<tr>
<td></td>
<td>C 20</td>
<td>10 102</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>64.1</td>
<td>3.7</td>
<td></td>
</tr>
<tr>
<td></td>
<td>D 40</td>
<td>10 206</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>51.8</td>
<td>4.3</td>
<td></td>
</tr>
<tr>
<td></td>
<td>E 20</td>
<td>20 213</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>54.6</td>
<td>3.6</td>
<td></td>
</tr>
<tr>
<td>Mass series</td>
<td>B 10</td>
<td>10 54</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>76.9</td>
<td>11.0</td>
<td></td>
</tr>
<tr>
<td></td>
<td>F 10</td>
<td>10 54</td>
<td>80 3.37</td>
<td>0.0103</td>
<td>107.0</td>
<td>15.2</td>
<td></td>
</tr>
<tr>
<td></td>
<td>G 10</td>
<td>10 54</td>
<td>150 3.37</td>
<td>0.0103</td>
<td>82.7</td>
<td>8.5</td>
<td></td>
</tr>
<tr>
<td>Bond series</td>
<td>H 20</td>
<td>10 102</td>
<td>10 3.37</td>
<td>0.0077</td>
<td>65.7</td>
<td>4.1</td>
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<tr>
<td></td>
<td>C 20</td>
<td>10 102</td>
<td>10 3.37</td>
<td>0.0103</td>
<td>64.1</td>
<td>3.7</td>
<td></td>
</tr>
<tr>
<td></td>
<td>I 20</td>
<td>10 102</td>
<td>10 3.37</td>
<td>0.0129</td>
<td>61.0</td>
<td>2.5</td>
<td></td>
</tr>
</tbody>
</table>

III. RESULTS AND DISCUSSION

The Kapitza conductance at the reference interface (sample A) is plotted as a function of temperature, where the conductance at the reference interface (sample A) is plotted as a function of temperature in both Figs. 1 and 2 (black squares) and the dashed lines are linear fits of the data. Each data point represents the mean result of five independent simulations and error bars represent the standard deviation of this average, i.e., repeatability. The systems were divided into 160 equally sized bins such that spatial temperature profiles could be calculated along the z-axis. Once in steady-state, time-averaged profiles were constructed from 4000 system snapshots taken over 2 × 10⁶ time steps (8.56 ns). A linear least-squares fit was then performed for each half of the domain. The five bins nearest to the bath and the interface were not included in these fits. The discontinuity between the fits at the interface, ΔT, was used to calculate hK through the relationship Q = hK ΔT.
standard deviation increases with increasing temperature due to the fact that our calculations are less sensitive to Kapitza conductance with increasing temperature (the temperature drop at the interface associated with Kapitza conductance decreases, while the temperature drops across the leads increases). Kapitza conductances at the interfaces contained within samples B through G (impurity distribution and mass series) were calculated as a function of temperature from 11 K to 50 K, and the conductances at the interfaces in samples H and I (bond series) were calculated at a fixed temperature of 30 K.

A. Influence of impurity distribution

The effects of the concentration and distribution of light impurities (mI = 10 amu) are shown in Fig. 1. When comparing the results from samples B, C, and D, it is clear that Kapitza conductance decreases with increasing impurity concentration; as in earlier works, increased interfacial disorder leads to lower realized values of Kapitza conductance, as well as a diminished temperature dependence. However, these data also show that the relationship between impurity concentration and the effective reduction in Kapitza conductance is non-linear; that is, doubling the number of impurities does not double the realized reduction in Kapitza conductance, which can be seen by comparing the difference in Kapitza conductance between B and C to the difference between C and D. This is consistent with the behavior observed in SiGe alloys, where increasing Ge concentration had a diminishing effect in terms of yielding lower values of thermal conductivity. However, in our earlier work in which substrates were chemically etched to vary interface roughness (i.e., interface disorder) we observed the opposite behavior, where relative reductions in Kapitza conductance increased with increasing disorder. Thus, taken collectively, these works serve to distinguish the effects of compositional and structural disorder. While both can be exploited to tune interfacial transport, the behavior of each is distinct.

B. Influence of impurity mass

The effect of impurity mass for a fixed distribution is shown in Fig. 2. Both light and heavy impurities (samples B and G, or mI = 10 amu and 150 amu, respectively) reduce conductance from the baseline values, albeit this reduction is not symmetric with impurity mass. Conventional forms of the phonon-impurity scattering rate are of the form \( \tau^{-1} \propto \left( \frac{m_{\text{host}} - m_I}{m_{\text{host}}} \right)^2 \). Thus, in a medium where the average atomic mass is 80 amu, 10 amu, and 150 amu impurities would behave identically. While this form of phonon scattering can hold in the context of thermal conductivity, the fact that it does not hold at an interface suggests other mechanisms are, in part, responsible for the observed behavior. Also shown in Fig. 2 is that when \( m_I \) falls between \( m_A \) and \( m_B \) (sample F, or \( m_I = 80 \text{ amu} \)), conductance increases, or, in other words, increased interfacial disorder increases the efficiency of thermal transport.

To further explore the mechanisms responsible for this observed behavior, we have calculated the local phonon DOS of each atom within the monolayers immediately adjacent to the interface. The DOS is proportional to the Fourier transform (\( \tilde{F} \)) of the velocity auto-correlation function (VACF) but in practice is calculated using standard estimation procedures for power spectral density. For each atom, the velocity is obtained at each integration time step to give a velocity fluctuation time series of 73 728 points. The Welch method of power spectral density estimation is then applied by creating eight 50% overlapping segments of 16 384 points to give an angular frequency resolution of \( 8.96 \times 10^{10} \text{ rad s}^{-1} \) based on our time step of 4.28 fs. Each segment is then multiplied by a Hamming window and the fast Fourier transform is computed. The power spectral density, equivalent to \( \tilde{F} \) (VACF), is then obtained by ensemble averaging the Fourier transform magnitudes of each segment. In order to compute the DOS in units of counts per frequency per volume, \( \tilde{F} \) (VACF) must be further normalized by the atomic mass, local temperature, and atomic density.

The phonon density of states of materials A and B, as well as those of 10, 80, and 150 amu impurities immediately adjacent to the interface (in samples B, F, and G, respectively) calculated at 11 K are plotted in Fig. 3(a). The primary spectral overlap between A and B falls between 5 and 7 Trad s\(^{-1}\). While both the 80 and 150 amu impurities exhibit spectral overlap within this range, the vibrational spectrum of the 10 amu impurity is largely outside the spectra of both materials A and B, thus providing insight as to why the 10 amu impurities produce lower realized values of Kapitza conductance as compared to 150 amu impurities. Again, according to Klemens theory, the strength of impurity scattering is proportional to \( \left( \frac{m_{\text{host}} - m_I}{m_{\text{host}}} \right)^2 \), which would suggest that the effects of 10 amu and 150 amu impurities should be the same. However, at an interface, where phonon scattering is not only dictated by a difference in absolute mass but also the overlap of phonon spectra, this does not hold. To further illustrate this point, we define the spectral overlap between material A, an impurity atom, and material B as
where $D_i(\omega)$ is the density of states of one of the three impurity atoms; this spectral overlap is plotted in Fig. 3(b). As is evident in the figure, while the overlap “width” of the 80 and the 150 amu impurities is similar, the area under the curve associated with the 80 amu impurity is larger (by $\approx 30\%$). In addition, the $A:80$ amu:$B$ overlap is centered about the inherent vibrational overlap between materials $A$ and $B$, thus indicating that the 80 amu impurities can serve to act as a “vibrational bridge” by creating a region of graded vibrational properties near the interface. However, this result is unique compared to earlier work in which a confined thin film at the interface served to grade the vibrational properties insofar as impurities enhance conductance at elevated temperatures, whereas the confined films only enhanced conductance at low temperatures ($\approx 10\%$ of the melt temperature, which in the present system is $<10\,K$).^{22}

**C. Influence of impurity bond**

Impurity atoms can differ not only in terms of atomic mass but also in terms of their bond characteristics, e.g., strength and radius. In a Lennard-Jones system, these characteristics are dictated by the energy and length parameters, $\epsilon$ and $\sigma$. In a dislocation free system, a change in either $\epsilon$ or $\sigma$ will have a similar effect insofar as it will change the interatomic force constant, $K = \partial^2 U / \partial r^2$. Thus, in order to assess the influence of the impurity bond characteristics, we chose to vary the Lennard-Jones energy parameter of 10 amu impurities, $\epsilon_i$, by $\pm 25\%$, while leaving $\sigma$ fixed (by keeping bond radius fixed, the coherent nature of the interfaces could be preserved). Lorentz-Berthelot mixing rules were applied for interactions between impurity and host atoms, $\epsilon_{ij} = \sqrt{\epsilon_i \epsilon_j}$, and Kapitza conductance was calculated at a fixed temperature of 30 K. As noted in Table I, changing $\epsilon_i$ by as much as $\pm 25\%$ led to no statistically significant change in Kapitza conductance, indicating for this combination of parameters, the mass of the impurity atoms plays the dominant role as compared to the impurity bond characteristics. This is consistent with earlier molecular dynamics studies of the thermal conductivity of SiGe alloys, where treating Ge atoms like heavy Si isotopes (ignoring differences in bond strength) did not distort results.^{38}

**IV. CONCLUSION**

In summary, we have investigated the influence of substitutional impurities on Kapitza conductance at coherent type interfaces via non-equilibrium molecular dynamics simulations. It has been shown that the presence of impurities at an interface can either increase or reduce the Kapitza conductance at an interface depending on the relative match or mismatch between the vibrational spectra of the materials comprising the interface and that of the impurities. These results suggest that at solid-solid interfaces between lattice-matched materials, e.g., AlAs:GaAs, compositional diffusivity (disorder) via either doping or alloying could enhance thermal transport.

**ACKNOWLEDGMENTS**

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